

# Scaling of xylem vessels and veins within the leaves of oak species

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**General models of plant vascular architecture, based on scaling of pipe diameters to remove the length dependence of hydraulic resistance within the xylem, have attracted strong interest. However, these models have neglected to consider the leaf, an important hydraulic component; they assume all leaves to have similar hydraulic properties, including similar pipe diameters in the petiole. We examine the scaling of the leaf xylem in 10 temperate oak species, an important hydraulic component. The mean hydraulic diameter of petiole xylem vessels varied by 30% among the 10 oak species. Conduit diameters narrowed from the petiole to the midrib to the secondary veins, consistent with resistance minimization, but the power function scaling exponent differed from that predicted for stems. Leaf size was an organizing trait within and across species. These findings indicate that leaf vasculature needs to be included in whole-plant scaling models, for these to accurately reflect and predict whole-plant transport and its implications for performance and ecology.**

**Keywords:** tapering; xylem vessels; hydraulic resistance; scaling relationships; allometry; stomatal density

## 1. INTRODUCTION

Plants need to deliver copious water to the leaf cells and airspaces via narrow conduits. If the entire vascular system comprised narrow conduits, its hydraulic resistance would be very high because conduit lumen resistance scales inversely with diameter raised to the fourth power (the Hagen–Poiseuille law; Tyree & Zimmermann 2002). Such a high hydraulic resistance would limit the degree to which stomata could remain open for photosynthesis at a given leaf water potential (Meinzer 2002). Trees have overcome this problem by developing vascular systems that have wider vessels in the trunk and branches than in the peripheral stems and leaves, and modelling optimal tapering has attracted substantial recent interest (West *et al.* 1999; McCulloh & Sperry 2005a,b; Coomes *et al.* 2006; Weitz *et al.* 2006). For convenience, these

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models have considered petioles as the end of the transport system (West *et al.* 1999). However, the leaf accounts for at least 30% of the plant resistance, and leaf venation architecture contributes to the determination of photosynthetic and transpiration rates (Sack *et al.* 2003; Brodribb *et al.* 2005, 2007; Sack & Holbrook 2006). Thus, a closer examination of scaling within leaves is important for predictions at the plant level.

Despite the importance of the leaf xylem, it might be legitimate to omit leaves from hydraulic scaling models if the xylem diameters of petioles (and veins) are invariant (e.g. West *et al.* 1999, box 1). Alternatively, the leaf xylem might simply follow the same scaling ‘rules’ as the stem. No study so far has tested whether the leaf xylem follows the trends proposed for the stem xylem scaling, i.e. that hydraulically weighted conduit lumen diameter ( $d_h$ ) tapers with branch diameter ( $D$ ) as  $d_h \propto D^\alpha$  (where optimal  $\alpha = 1/6$ ; Anfodillo *et al.* 2006; Coomes *et al.* 2006). In fact, the leaf xylem may follow different rules given its different structure and function, e.g. its reticulation and leakiness to the mesophyll surrounding the veins (McCulloh & Sperry 2005a,b).

We examined scaling relationships within the leaf vasculature of 10 temperate oak species (*Quercus*, Fagaceae). For a given species, and across species, we hypothesized that there would be tapering of  $d_h$  in petiole, midrib and secondary veins, and of vascular bundles within veins. Further, we hypothesized that the  $d_h$  would increase with leaf size within and across species. Additionally, we tested whether the leaf xylem vessel properties correlate across species with key functional traits, stomatal density (SD) and leaf mass per unit area (LMA).

## 2. MATERIAL AND METHODS

Leaves from 10 oak species were sampled from the University Botanic Garden, Cambridge, UK and the Sir Harold Hillier Gardens, Hampshire, UK. Most of these trees were planted within the last 30 years and their diameters at breast height ranged from 1.2 to 141 cm (mean 40 cm). We sampled disease-free leaves from a sun-exposed, south-facing branch for five trees per species. Lamina areas were determined from digital images using IMAGEJ (<http://rsb.info.nih.gov/ij/>). We determined the SD using nail varnish imprints of the abaxial leaf surfaces; we counted stomata within three areas of the peel under an optical microscope ( $\times 100$ ; L3000B-HTG, GX Optical, China). LMA was determined by dividing leaf area by mass after drying the leaves for 72 hours at 70°C.

We estimated the diameters of the vascular bundles and vessels from cross-sections at (i) the midpoint of the petiole, (ii) one-third of the way along the midrib, and (iii) one-third of the way along the secondary vein branching closest to the point at which the midrib was cut. We stained the sections with Safranin O (0.01%), for imaging and measurement of diameters of vessel lumens and vascular bundles (including fibres) using a confocal microscope with an Argon laser and analysis software (TCSSP2 model, Leica Microsystems, Germany). The hydraulic conductance of a pipe scales as the fourth power of lumen diameter ( $d$ ), so we calculated a hydraulically weighted mean diameter,  $d_h = \sum d^5 / \sum d^4$  (Mencuccini *et al.* 1997; Anfodillo *et al.* 2006), using all vessels with a diameter greater than half that of the largest vessel in each sample to eliminate vessels that appear to be narrow because the tapering ends have been sampled (James *et al.* 2003), and the number of such vessels within a bundle was counted ( $N$ ).

We determined the scaling of  $d_h$  and the vascular bundle diameter  $D$  by fitting straight lines to log–log transformed data (i.e. allometric relationships) by using the standard major axis regression (SMA; using the SMATR package in the R statistics software); this also allowed a comparison of whether slopes ( $\alpha$  values) and intercepts differed among species. The SMA

Table 1. Petiole xylem characteristics of the 10 temperate oak species, including hydraulically weighted mean vessel diameter ( $d_h$ ), vascular bundle diameter ( $D$ ) and number of vessels ( $N$ ), as well as the mean individual leaf area (area), LMA and SD. (The final column contains the scaling exponent of the power functions shown in figure 1. All of these properties varied significantly among species (ANOVA,  $p < 0.05$ ). n.d., not determined because leaves were hirsute.)

code	species	$d_h$ ( $\mu\text{m}$ )	$N$ (no. $\text{mm}^{-2}$ )	$D$ ( $\mu\text{m}$ )	area ( $\text{cm}^2$ )	LMA ( $\text{g m}^{-2}$ )	SD (no. $\text{mm}^{-2}$ )	$\alpha$ values
1	<i>Q. castaneifolia</i>	27.4	25.6	968	56	105	332	0.55
2	<i>Q. cerris</i>	25.5	51.8	711	26	87	515	0.59
3	<i>Q. georgiana</i>	22.4	51.5	670	22	74	752	0.58
4	<i>Q. ilex</i>	21.2	21.2	705	22	104	n.d.	0.73
5	<i>Q. nigra</i>	26.1	19.2	886	30	74	525	0.48
6	<i>Q. petraea</i>	28.2	27.4	1217	85	49	228	0.42
7	<i>Q. rhysophylla</i>	26.8	31.2	1505	74	110	761	0.47
8	<i>Q. robur</i>	25.5	30.0	1222	61	54	275	0.48
9	<i>Q. rubra</i>	34.0	30.4	1132	128	81	493	0.51
10	<i>Q. serrata</i>	30.6	36.6	847	59	74	653	0.60

regression was also used to fit lines to non-transformed data (i.e. isometric relationships).

### 3. RESULTS

We found a substantial variation across the 10 oak species in petiole xylem characters:  $d_h$  varied from 21 to 34  $\mu\text{m}$ ; vascular bundle diameter varied from 670 to 1505  $\mu\text{m}$ ; and the vessel number per area of vascular bundle varied from 19 to 52  $\text{mm}^{-2}$  (table 1). Species also varied strongly in these properties for the midrib and secondary veins (figures 1 and 2 and figure A1 in the electronic supplementary material).

Within and across the 10 species, there were strong scaling relationships between  $d_h$  and  $D$  (figures 1 and 2). Within and across species,  $d_h$  correlated with  $D$  for petioles, midribs and secondary veins (figure A1 in the electronic supplementary material, figure 1*a–c*); additionally, the  $D$  of petioles, midribs and secondary veins were intercorrelated (figure 1*d–f*), as were the  $d_h$  in petioles, midribs and secondary veins (figure 1*g–i*). Across vein orders, for all the 10 species,  $d_h$  scaled with  $D$ , with  $\alpha$  values of 0.42–0.73, substantially greater than the 1/6 predicted by scaling models for stems (figure 1; table 1).

Across species,  $d_h$  and  $D$  of petioles, midribs and secondary veins scaled tightly with mean leaf area (figure 2). The species'  $\alpha$  values correlated negatively with the leaf area, indicating a steeper conduit tapering in smaller leaves (table 1; Spearman's rank test,  $p = 0.032$ ). The leaf xylem properties were not correlated with LMA, SD or the average size of the adult tree (figure 2).

### 4. DISCUSSION

It is now widely acknowledged that the narrowing of conduit diameters towards the periphery of bulk transport systems reduces the dependency of hydraulic resistance on path length (Becker *et al.* 2000), but controversy remains over which processes need to be included in models in order to accurately predict the scaling of  $d_h$  and  $D$ . The pioneering model of West *et al.* (1999) predicts that the length dependence of hydraulic resistance is practically removed from branching stem systems when  $d_h \propto D^{1/6}$ , assuming that the system comprises continuous non-leaky

pipes running from trunk to the petioles and that branching systems are fractal-like and volume filling (West *et al.* 1999; Becker *et al.* 2000; Anfodillo *et al.* 2006). We have shown strong relationships between  $d_h$  and  $D$  for the leaf vasculature of the 10 oak species with scaling exponents consistently greater than 1/6. Several factors will need to be considered in the derivation of a theoretical model of vascular architecture for leaves as distinct from that of stems. Leaf venation is approximately plane filling and typically reticulate (Pelletier & Turcotte 2000). Also, leaf venation is laterally 'leaky' to the surroundings (McCulloh & Sperry 2005*a,b*; Zwieniecki *et al.* 2006); the tapering of vascular bundles within pine needles is optimized to enable even delivery of water along their length (Zwieniecki *et al.* 2006). In addition, the cost of constructing the vascular system needs to be considered to determine the theoretically optimal scaling of  $d_h$  with  $D$  (McCulloh & Sperry 2005*a,b*). Further investigation is needed of the developmental, hydraulic and economic factors that would determine the optimal tapering of leaf xylem conduits.

Our observations of general scaling between leaf size and vascular properties are consistent with early demonstrations that the leaf area correlates with the petiole vessel diameter for a given species (Salisbury 1913). This scaling supports the classical principle that larger leaves would require a larger 'pipe' system to supply a greater transpiration surface (cf. Shinozaki *et al.* 1964). We also found that the scaling of  $d_h$  with  $D$  itself scaled with the leaf size across species. More work is needed to determine how far phylogenetically diverse species depart from the scaling trends found for the 10 oak species. The lack of coordination between  $d_h$  and  $D$  and SD or LMA needs to be confirmed across diverse species sets.

The  $d_h$  values given here are within the range reported previously for other tree species (Cochard *et al.* 2004; Nardini *et al.* 2005; Sack & Frole 2006), for which the leaf hydraulic conductance was low, 2–20  $\text{mmol m}^{-2} \text{s}^{-1} \text{MPa}^{-1}$ , thus accounting for a major portion of whole-plant resistance. Because the leaf xylem scales differently from tree stem xylem, and species differ in the leaf xylem properties

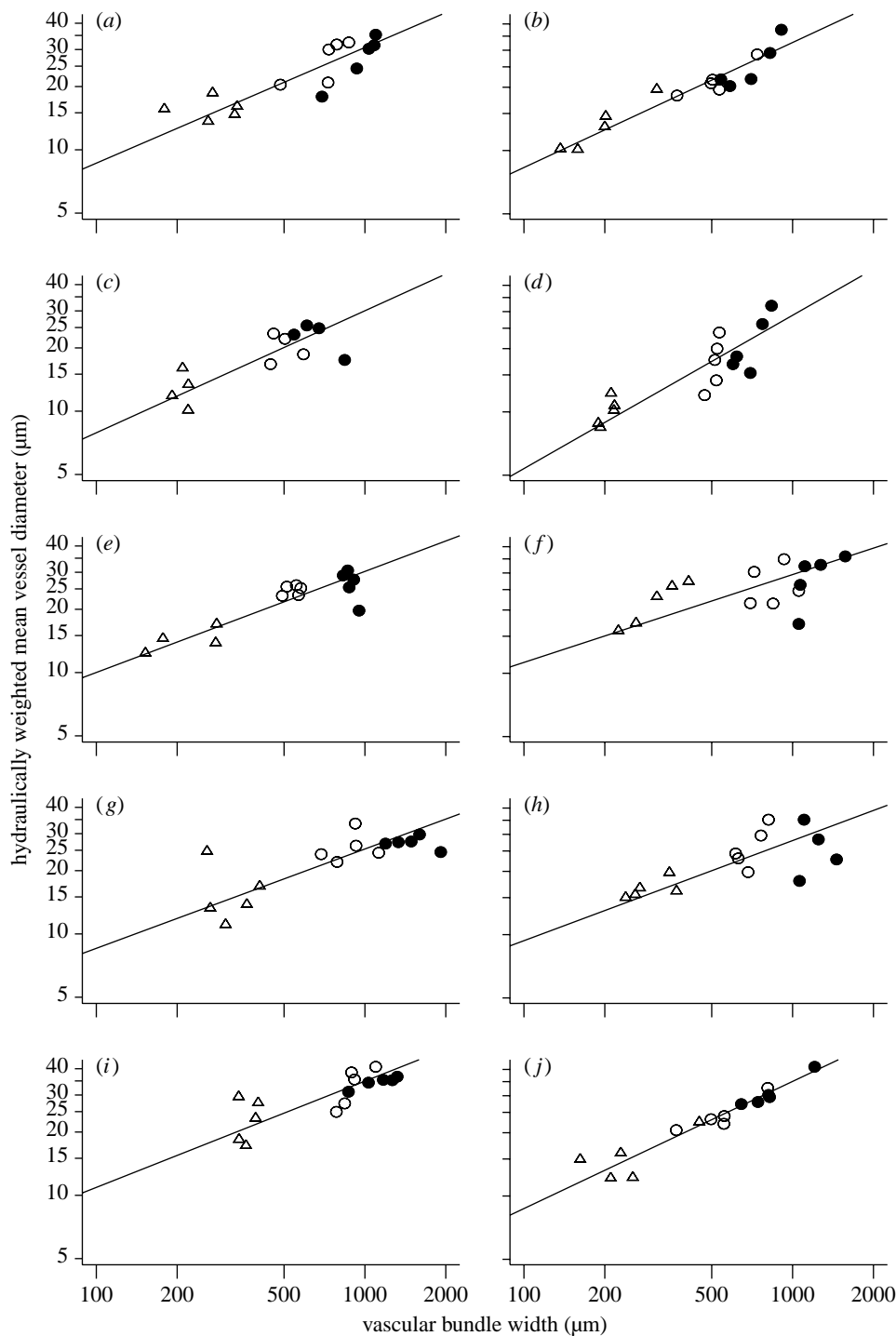


Figure 1. Scaling of hydraulically weighted vessel diameter ( $d_h$ ) with vascular bundle diameter ( $D$ ) within 10 species of oak; standard major axes were fitted to the data. Vessels were sampled from the following: open circles, primary vein; triangles, secondary vein; and filled circles, petiole. (a) *Quercus castaneifolia*:  $d_h = 0.67D^{0.55}$  and  $r = 0.87$ ,  $p < 0.001$ ; (b) *Q. cerris*:  $d_h = 0.52D^{0.59}$  and  $r = 0.93$ ,  $p < 0.001$ ; (c) *Q. georgiana*:  $d_h = 0.53D^{0.58}$  and  $r = 0.68$ ,  $p < 0.001$ ; (d) *Q. ilex*:  $d_h = 0.18D^{0.72}$  and  $r = 0.85$ ,  $p < 0.001$ ; (e) *Q. nigra*:  $d_h = 1.07D^{0.48}$  and  $r = 0.78$ ,  $p < 0.001$ ; (f) *Q. petraea*:  $d_h = 1.61D^{0.42}$  and  $r = 0.61$ ,  $p < 0.001$ ; (g) *Q. rhysophylla*:  $d_h = 0.95D^{0.47}$  and  $r = 0.67$ ,  $p < 0.001$ ; (h) *Q. robur*:  $d_h = 1.02D^{0.47}$  and  $r = 0.58$ ,  $p = 0.001$ ; (i) *Q. rubra*:  $d_h = 1.05D^{0.51}$  and  $r = 0.81$ ,  $p < 0.001$ ; and (j) *Q. serrata*:  $d_h = 0.52D^{0.60}$  and  $r = 0.98$ ,  $p < 0.001$ .

sufficiently to influence their whole-plant hydraulic resistance, realistic models of whole-plant vasculature should explicitly include the scaling of leaf venation architecture.

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Anfodillo, T., Carraro, V., Carrer, M., Fior, C. & Rossi, S. 2006 Convergent tapering of xylem vessels in different woody species. *New Phytol.* **169**, 279–290. (doi:10.1111/j.1469-8137.2005.01587.x)

Becker, P., Gribben, R. J. & Lim, C. M. 2000 Tapered conduits can buffer hydraulic conductance from path-length effects. *Tree Physiol.* **20**, 965–967.

Brodribb, T. J., Holbrook, N. M., Zwieniecki, M. A. & Palma, B. 2005 Leaf hydraulic capacity in ferns, conifers

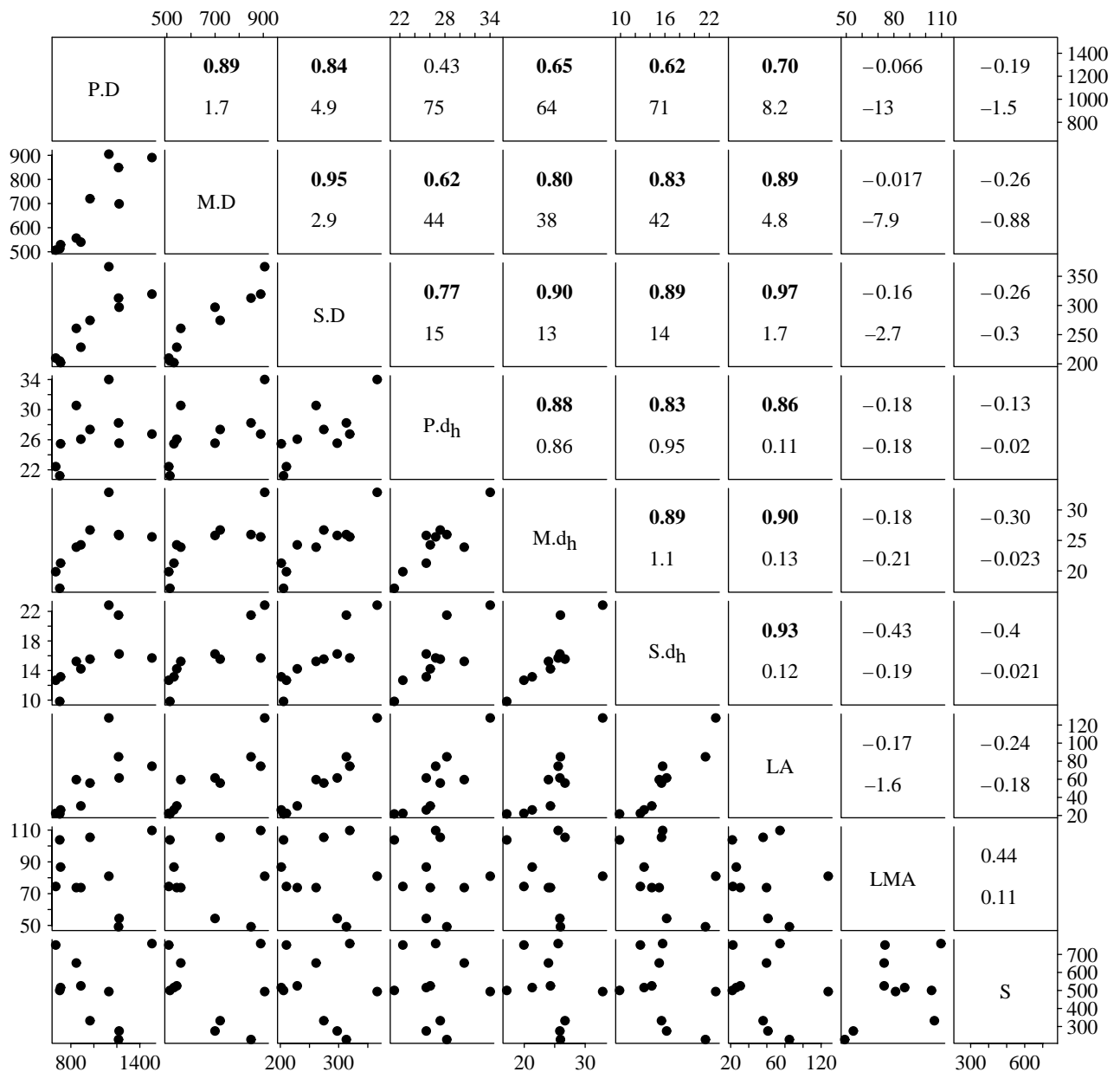


Figure 2. Correlations among foliar traits measured for 10 species of oak. The upper right panels contain Pearson correlation coefficients (upper number, all values in bold are greater than 0.60 and significant at  $p < 0.05$ ) and SMA slopes (lower number); none of the variables were transformed. The lower left panels show the data points. The traits are abbreviated along the diagonal as follows: P.D, petiole vein diameter; M.D, midrib vein diameter; S.D, secondary vein diameter; P.d<sub>h</sub>, petiole vessel mean hydraulically weighted diameter; M.d<sub>h</sub>, midrib vessel mean hydraulically weighted diameter; S.d<sub>h</sub>, secondary vessel mean hydraulically weighted diameter; LA, leaf area; LMA, leaf mass per unit area; S, stomatal density.

- and angiosperms: impacts on photosynthetic maxima. *New Phytol.* **165**, 839–846. (doi:10.1111/j.1469-8137.2004.01259.x)
- Brodribb, T. J., Feild, T. S. & Jordan, G. J. 2007 Leaf maximum photosynthetic rate and venation are linked by hydraulics. *Plant Physiol.* **144**, 1890–1898. (doi:10.1104/pp.107.101352)
- Cochard, H., Nardini, A. & Coll, L. 2004 Hydraulic architecture of leaf blades: where is the main resistance? *Plant Cell Environ.* **27**, 1257–1267. (doi:10.1111/j.1365-3040.2004.01233.x)
- Coomes, D. A., Jenkins, K. L. & Cole, E. S. 2006 Scaling of tree vascular transport systems along gradients of nutrient supply and altitude. *Biol. Lett.* **3**, 86–89. (doi:10.1098/rsbl.2006.0551)
- James, S. A., Meinzer, F. C., Goldstein, G., Woodruff, D., Jones, T., Restom, T., Mejia, M., Clearwater, M. & Campanello, P. 2003 Axial and radial water transport and internal water storage in tropical forest canopy trees. *Oecologia* **134**, 37–45. (doi:10.1007/s00442-002-1080-8)
- McCulloh, K. A. & Sperry, J. S. 2005a Patterns in hydraulic architecture and their implications for transport efficiency. *Tree Physiol.* **25**, 257–267.
- McCulloh, K. A. & Sperry, J. S. 2005b The evaluation of Murray's law in *Psilotum nudum* (Psilotaceae), an analogue of ancestral vascular plants. *Am. J. Bot.* **92**, 985–989. (doi:10.3732/ajb.92.6.985)
- Meinzer, F. C. 2002 Co-ordination of vapour and liquid phase water transport properties in plants. *Plant Cell Environ.* **25**, 265–274. (doi:10.1046/j.1365-3040.2002.00781.x)
- Mencuccini, M., Grace, J. & Fioravanti, M. 1997 Bio-mechanical and hydraulic determinants of the tree structure in Scots pine: anatomical characteristics. *Tree Physiol.* **17**, 105–113.

- Nardini, A., Gortan, E. & Salleo, S. 2005 Hydraulic efficiency of the leaf venation system in sun- and shade-adapted species. *Funct. Plant Biol.* **32**, 953–961. (doi:10.1071/FP05100)
- Pelletier, J. D. & Turcotte, D. L. 2000 Shapes of river networks and leaves: are they statistically similar? *Phil. Trans. R. Soc. B* **355**, 307–311. (doi:10.1098/rstb.2000.0566)
- Sack, L. & Frole, K. 2006 Leaf structural diversity is related to hydraulic capacity in tropical rain forest trees. *Ecology* **87**, 483–491. (doi:10.1890/05-0710)
- Sack, L. & Holbrook, N. M. 2006 Leaf hydraulics. *Annu. Rev. Plant Biol.* **57**, 361–381. (doi:10.1146/annurev.arplant.56.032604.144141)
- Sack, L., Cowan, P. D., Jaikumar, N. & Holbrook, N. M. 2003 The ‘hydrology’ of leaves: co-ordination of structure and function in temperate woody species. *Plant Cell Environ.* **26**, 1343–1356. (doi:10.1046/j.0016-8025.2003.01058.x)
- Salisbury, E. J. 1913 The determining factors in petiolar structure. *New Phytol.* **12**, 281–289. (doi:10.1111/j.1469-8137.1913.tb05705.x)
- Shinozaki, K., Yoda, K., Hozumi, K. & Kira, T. 1964 A quantitative analysis of plant form—the pipe model theory. *Jpn J. Ecol.* **14**, 97–105.
- Tyree, M. T. & Zimmermann, M. H. 2002 *Xylem structure and the ascent of sap*. Berlin, Germany: Springer.
- Weitz, J. S., Ogle, K. & Horn, H. S. 2006 Ontogenetically stable hydraulic design in woody plants. *Funct. Ecol.* **20**, 191–199. (doi:10.1111/j.1365-2435.2006.01083.x)
- West, G. B., Brown, J. H. & Enquist, B. J. 1999 A general model for the structure and allometry of plant vascular systems. *Nature* **400**, 664–667. (doi:10.1038/23251)
- Zwieniecki, M. A., Stone, H. A., Leigh, A., Boyce, C. K. & Holbrook, N. M. 2006 Hydraulic design of pine needles: one-dimensional optimization for single-vein leaves. *Plant Cell Environ.* **29**, 803–809. (doi:10.1111/j.1365-3040.2005.01448.x)